2.4 Factor and Solve Polynomial Equations

Monday, November 27, 2017 6:58 AM

Polynomial is factored completely if it is written as a product of unfactorable polynomials with integer coefficients.

Common Monomial Factor

Example A)	$x^3 + 2x^2 - 15x = x(x^2 + 2x - 15)$	Factor common monomial
	=x(x+5)(x-3)	Factor Trinomial

Example B)
$$2x^5 - 18x^3 = 2x^3(x^2 - 9)$$
 Factor common monomial $= 2x^3(x+3)(x-3)$ Difference of two squares

Example C)	$4x^4 - 16x^3 + 16x^2 = 4x^2(x^2 - 4x + 4)$	Factor common monomial
	$= 4x^{2}(x-2)(x-2)$ $= 4x^{2}(x-2)^{2}$	Perfect Square Trinomial

Special Factoring Patterns

Sum of Two Cubes

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$
 $8x^3 + 27 = (2x+3)(4x^2 - 6x + 9)$

Difference of Two Cubes

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$
 $64x^3 - 1 = (4x - 1)(16x^2 + 4x + 1)$

List of Cubes:

$$1^{3} = 1$$
 $2^{3} = 8$
 $3^{3} = 27$
 $4^{3} = 64$
 $5^{3} = 125$
 $6^{3} = 216$
 $7^{3} = 343$
 $8^{3} = 512$
 $9^{3} = 729$
 $10^{3} = 1000$

Factor by Grouping

$$x^3 - 3x^2 - 16x + 48$$

$(x^3-3x^2)(-16x+48)$	Make two groups
$x^2(x-3) - 16(x-3)$	Factor each group separately
$(x-3)(x^2-16)$	Factor again
(x-3)(x+4)(x-4)	Difference of two squares

Factor polynomials in quadratic form

Example A)

$16x^4 - 81$	Difference of two Squares
$(4x^2+9)(4x^2-9)$	Difference of two Squares
$(4x^2+9)(2x+3)(2x-3)$	

Example B)

$2x^8 + 10x^5 + 12x^2$	Factor out common monomial
$2x^2(x^6 + 5x^3 + 6)$	Factor trinomial in quadratic form
$2x^2(x^3+3)(x^3+2)$	